Firm-level comparative advantage☆
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1. Introduction

There is a wealth of empirical evidence that factor intensity differs across firms within the same country–industry group. For instance, in our data, comprising more than 300,000 European firms, only 30% of the total variance in firm-level capital/labor ratios is between country–industry groups, 70% is within the same country–industry groups. Empirical literature in international trade has documented that differences in factor intensities matter for firms’ performances (e.g. Bernard, Jensen, Redding and Schott 2007). These observations contrast with the assumption usually adopted in trade models whereby firms either are assumed to be identical or are assumed to differ by Hicks-neutral productivity. In either case, the resulting factor intensities are identical across firms within any industry. Following this empirical observation, we consider a Heckscher–Ohlin model in which firms differ in the relative marginal productivity of factors. As a result, firms have different factor intensities even within the same country–industry group.

The main result emerging from this model is that countries’ comparative advantage begets a comparative advantage at firm level. The three key firm-level variables in the model are relative capital/labor ratio ($\kappa$), relative marginal costs, and relative sales; all three relative to the industry average. We say that a firm has a comparative advantage over another if the first firm’s relative marginal cost is lower than the relative marginal cost of the second firm. Our main theoretical result may be stated as follows:

Consider any two firms with same $\kappa$ but belonging to different countries and industries. The firm that is intensive in the factor intensively used in its industry and of which its country is relatively well-endowed has a comparative advantage over the other firm. Because of the comparative advantage, the firm will also have higher relative sales.

The statement above is the natural generalization of the Heckscher–Ohlin theorem to an environment with heterogeneous firms. In the Heckscher–Ohlin theorem, the comparative advantage of a country is determined by the matching between the characteristics of countries and those of industries. In the statement above, the comparative advantage of a firm is determined by the matching between its characteristics ($\kappa$) and those of the industry and country to which it belongs. In the Heckscher–Ohlin theorem, the comparative advantage of countries gives rise to differences in the relative size of industry output (international specialization). In the statement above, the comparative advantage of firms gives rise to differences in the relative size of firm output (relative sales).

As an example, consider two firms in different industries and different countries but with an identical $\kappa$. Assume, for instance, $\kappa > 1$. Then,
the firm in the capital intensive industry and capital abundant country will have a comparative advantage (lower relative marginal cost) over the firm in another industry and country. The firm's comparative advantage will show up in larger relative sales. If, instead, we consider two firms whose capital intensity is lower than their respective country–industry average (κ < 1) then the firm in the capital intensive industry and capital abundant country will have a comparative disadvantage and lower relative sales. This prediction does not obtain in models where heterogeneity is Hicks-neutral. In these models, two firms with same relative productivity but in different countries and industries have identical relative marginal cost and identical relative sales.

Our empirical investigation, conducted on a dataset which comprises about 300,000 firms in 21 European countries and 95 industries, strongly supports the theoretical result. Both structural and non-structural estimates show that the relationship between relative sales and relative factor intensity is affected by comparative advantage in the way predicted by the model. For instance, the non-structural estimates show that firms with capital intensity ten percent above their respective country–industry average (κ = 1.1) have different relative sales: the sales of firms in a capital intensive industry and a capital abundant country are 2.68% larger than the average firm in the same country–industry whereas the sales of firms in a labor intensive industry and a labor abundant country are only 1.66% larger than the average firm in the same country–industry.

We are not alone to assume heterogeneity in factor intensity. Costinot and Vogel (2010) and Burstein and Vogel (2012) are notable examples. Their models differ from ours in terms of the market structure, technology, and preferences. The focuses are also very different; they (as well as Vannoothenberge, 2011, who uses a model structure similar to ours) study the effect of trade liberalization on wage inequality, we study instead how country comparative advantage begets comparative advantage at firm level. There are also differences in the mechanisms driving the results; in these three papers results rest on skilled biased heterogeneity, ours do not. Yet, in their works like in ours, heterogeneity in factor intensity harnessed to a better extent the potentials of heterogeneous firm models in the understanding of international trade issues.

Our paper contributes to the literature in two ways. First, it provides a novel approach to the verification of the Heckscher–Ohlin (HO) model. Seminal contributions, e.g., Learner (1980), Treffler (1993, 1995) Davis and Weinstein (2001) and Romalis (2004) have provided solid evidence on the empirical merits of the factors proportion theory. In their works, comparative advantage is revealed by the effect it has on aggregate variables (the factor content of trade or industry specialization). We propose a different approach. In our model, comparative advantage is revealed by the effect it has on firm-level variables. Comparative advantage is the mechanism driving the HO theorem but it remains behind the scenes in homogenous-firm models, as well as in Hicks-neutral heterogeneity models, because it does not give rise to a comparative advantage at firm level. Being able to observe the firm-level comparative advantage generated by the comparative advantage of countries brings to light the fundamental mechanism driving the HO theorem. Approaches based on aggregate variables are, of course, unsuited to bring this mechanism to light.

Our second contribution is to show that countries' comparative advantage matters for explaining relative performances within industries. Seminal contributions by Bernard et al. (2003) and Melitz (2003) as well as many subsequent important developments use a one factor model and take out countries' comparative advantage. They are therefore unsuited to study the effect of country' comparative advantage on firm performances. Bernard, Redding and Schott (2007) are the first to introduce firm heterogeneity in a HO model but they consider only Hicks-neutral productivity differences. When productivity differences are Hicks-neutral the comparative advantage of countries does not influence firm relative sales within an industry. Thus, the one-factor assumption or Hicks-neutral heterogeneity makes that within-industry relative performances are independent from comparative advantage and depend only on exogenously given differences in productivity. As a result, one may be left with the impression that there is a dichotomy between within-industry effects and across-industry effects, the former being driven by firm-level differences and the latter by countries' comparative advantage. Our work, instead, highlights precisely how within-industry effects are determined jointly by firm-level characteristics (κ) and countries' comparative advantage.

We conclude this section by mentioning that the four core theorems of international trade remain valid in our model. But the degree of international specialization, the intensity of the Stolper–Samuelson and Rybczynski magnification effects, and the size of the factor price equalization set are all affected. We briefly present these results in Section S2.9.2 of the online supplement.

The remainder of the paper is as follows. Section 2 outlines the model, Section 3 describes the theoretical results, Section 4 derives the estimable equation, Section 5 presents the data, Sections 6 and 7 present the empirical results for the structural and non-structural estimates respectively, and Section 8 concludes. The online supplement, Sect. 9, contains the detailed description of the model, proofs of the results, and further technical matters.

2. Heterogeneity

We extend the model in Bernard, Redding and Schott (2007) by assuming firm heterogeneity in factor intensity. In this section we focus on the essential features of the model which we detail in Section 9.1 of the online supplement.

The world economy is composed of two countries indexed by c = H, F; it produces two differentiated goods indexed by i = Y, Z by using two primary factors indexed by j = K, L. Each country is endowed with a share τj > 0 of world's endowments, R and L. Production requires fixed and variable inputs in each period. The variable input technology takes the CES form here represented by the marginal cost which, for a firm in industry i of country c, is

\[ mc_i (\phi, \beta) = \phi \left[ (1 - \lambda_i) \sigma (w^c)^{1-\sigma} (1 - \lambda_i) \sigma (\frac{\sigma}{\beta}) \right] \]

where λi ∈ (0,1) is a constant technology parameter of industry i, \( w^c \) denote, respectively, the price of K and L in country c, and \( \sigma > 1 \) measures gross substitutability between factors. The variable \( \phi \) captures Hicks-neutral productivity differences across firms. The variable \( \beta \) captures differences across firms in the relative marginal productivity of factors. Models that focus on Hicks-neutral heterogeneity let \( \phi \) vary across firms but assume \( \beta \) identical across firms. We instead let both \( \phi \) and \( \beta \) vary across firms. We let \( \phi \) and \( \beta \) be independent random variables with cumulative distribution \( V(\phi) \) and \( G(\beta) \) both with support (0,∞).

The optimal \( K \)-intensity in production, \( \theta_0(\beta) \), is

\[ \theta_0(\beta) = (\sigma \phi)^\sigma \Lambda(\beta + 1)^{-\gamma} \]

where \( \sigma \phi \equiv w^c/\phi \) and \( \Lambda \equiv (1 - \lambda_i)/\lambda_i \). Obviously, \( \theta_0(\beta) \) is independent from the Hicks-neutral shifter \( \phi \).

By paying a fixed entry cost, a firm draws randomly one of the random variables and remains married to it until death of the firm do them apart (like in all the heterogeneous firm literature). The other
variable instead is a random shock hitting continuously the production process of the firm. This assumption captures the idea that although an initial investment in fixed entry cost gives the firm an information on its marginal cost (this is represented in the model by the costly draw of one of the stochastic variables), the actual marginal cost of every production experience is not known until production is actually taking place (random shock to the production process). It is irrelevant to the results of the model which variable has a life-time association with the firm. For the sake of expositional clarity, we assume that by paying a fixed entry cost a firm draws $\beta$ and remains associated with it until death. Furthermore, at any point in time the firm is hit by a particular realization of $\phi$ and as a probability of death equal to $\tilde{\phi}$.3

Turning to the fixed input technology, whether it is homogenous or heterogeneous across firms gives qualitatively the same results. We assume homogenous fixed costs since this assumption allows focusing on heterogeneity in the production process (which is the heart of the matter). This is the assumption most commonly retained in the literature (Melitz, 2003; Bernard, Redding and Schott, 2007; and many others). Specifically we assume that the fixed input technology is represented by the cost function $mc_i$ described below in Eq. (3). Thus, the fixed production cost is $F_i mc_i$ where $F_i$ is a positive constant. This assumption represents the fixed input as a homogenous, non-traded, composite good produced in a perfectly competitive market by assembling in a CES all varieties of the domestic industry output (similarly to Ethier, 1982). But it may also be interpreted as in Yeaple (2005) who assumes that the fixed cost is represented by output that must be produced by the firm and that ultimately cannot be sold; with the difference that in our model this output requires a unit cost function $mc_i$. Analogously to fixed production cost, the fixed exporting cost is $F_i mc_i$ and the fixed export cost is $F_i mc_i$ where $F_i$ and $F_e$ are positive constant. Fixed entry cost is paid in order to draw $\beta$, fixed exporting costs are paid in order to access the foreign market.

Two remarks are useful at this point. The first remark concerns all the fixed cost. Fixed exporting costs are not necessary in our model. Thus, we present our results in the main text under the assumption that $F_e=0$. This makes the reading smoother by simplifying the notation but, more importantly, highlights that our results do not depend on the partitioning of firms by export status. We think this is quite interesting because many results in the literature (especially the literature on the skill premium) hinge on the existence of the partitioning of firms by export status.4 For completeness of investigation we shall reintroduce fixed exporting costs in Section 9.3 of the online supplement where we show that our results remain valid. Fixed entry and fixed production cost result in firm selection. This selection is not necessary in our model but we keep it since we find interesting the fact that the entry process makes firm-level comparative advantage hold a fortiori. In any case, if we assume that all firms survive in the market (as in Burstein and Vogel, 2012) the results would remain unchanged (see Section 9.2.6 of the online supplement). The second remark concerns the relationship between sales and $K$-intensity. We see from expression (1) and (2) that higher $K$-intensity corresponds to a lower marginal cost and, therefore, to higher sales. This positive correlation between sales and $K$-intensity is what we find in our data.5 However, nothing in our model hinges on this positive relationship. In the appendix we show that assuming a negative relationship between $K$-intensity and sales leaves our results unchanged (see Section 9.2.8 of the online supplement).

After drawing $\beta$ the firm stays in the market if the expected realization of profits is non-negative and exits otherwise.6 Let $\beta^*$ be the least value of $\beta$ in industry $c$ of country $c$ such that the expected realization of profit after having drawn $\beta$ is zero. Let $\bar{\phi} \equiv \left( \int_0^\phi \phi^{\alpha-1} d\phi \right)^\alpha$ and $\beta^\ast_c \equiv \left( \int_0^{\beta^\ast_c} \beta^{\alpha-1} d\beta \right)^\alpha$. Furthermore, let the average $K$-intensity and the average marginal cost in industry $i$ of country $c$ be defined respectively as $\bar{mc}_i^c \equiv \left\{ \int_0^\infty \left( mc_i^c(\phi, \beta) \right)^{\alpha-1} d\phi \right\}^{\frac{\alpha}{\alpha-1}}$ and $\bar{mc}_i^c \equiv \left\{ \int_0^\infty \beta^{\alpha-1} d\beta \right\}^{\alpha}$. Then, we have

$$\bar{mc}_i^c = \frac{1}{\bar{\phi}} \left[ \left( \lambda_i \right)^{\alpha-1} + (1-\lambda_i)^{\alpha-1} \left( \bar{\beta}_i \right)^{\alpha-1} \right]^{\frac{\alpha}{\alpha-1}}, \quad (3)$$

$$\bar{mc}_i^c = \left( \alpha \right)^{\alpha} \left( \tilde{\phi} \right)^{\alpha-1}, \quad (4)$$

where, given that some firms decide not to stay in the market, $\beta^\ast_c$ becomes equal to $\left( \frac{1}{\bar{\phi}} \right) \int_0^\infty \beta^{\alpha-1} d\beta$. Incidentally, for future reference note that $\bar{mc}_i^c = mc_i^c (\phi, \beta)$. A further remark is useful at this point. In models where firms are homogenous or heterogeneous with identical factor intensity the average factor intensity is $\left( \alpha \right)^{\alpha} \lambda^\alpha$. We can see from expression (4) that, with respect to those models, there is a factor bias in our model whenever $\beta^\ast_c \neq 1$. The bias is endogenous since it depends on the cut-off values $\beta^\ast_c$. It may go in either direction – to a $K$-bias or to a $L$-bias – and the direction may differ in different industries or countries. None of our results depend on the direction or on the existence of such bias (see through Section 9.2 of the online supplement).

Turning to demand, the representative consumer has Dixit–Stiglitz preferences represented by a Cobb–Douglas index, with shares $\gamma_1 = (0,1)$, $\gamma_2 = 1$, and defined over CES aggregates whose elasticity of substitution between varieties is $\omega > 1$.

### 3. Comparative advantage

To fix ideas, throughout the paper it is assumed that country $H$ is $K$-abundant, i.e., $v_H^1 > v_Y^1$, and that industry $Y$ is $K$-intensive, i.e., $A_Y > A_H$.7

Our objective is to show that countries’ comparative advantage generates a comparative advantage at firm level. We begin by four definitions.

Let $a_Y^c \equiv \left( A_Y \right)^{\alpha} (\alpha)^{\alpha-1} \left( \beta_i \right)^{\alpha-1}$. Note $a_Y^c > a_Y$ since $H$ is $K$-abundant, $Y$ is $K$-intensive and (as shown in Section 9.2.1 of the online supplement) $\bar{\beta}_1 > \bar{\beta}_2$.

**Definition 1.** Let $a \equiv A = \left( a_Y^c, a_Y \right)$. Then $a$ is an index of comparative advantage of countries.

**Definition 2.** Let $\kappa$ denote the relative $K$-intensity and let $\psi$ denote the relative Hicks-neutral productivity, i.e.,

$$\kappa \equiv \frac{\beta_i}{\bar{\beta}_i} = \left( \frac{\beta_i}{\bar{\beta}_i} \right)^{\alpha-1}, \quad \varphi \equiv \frac{\bar{mc}_i^c}{mc_i^c} \left( \frac{\beta_i}{\bar{\beta}_i} \right)^{\alpha-1} \quad (5)$$

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3 Other modeling choices are possible and would leave the results unchanged. For instance, we could assume that both $\phi$ and $\beta$ remain attached to the firm until death (as in Harrigan and Reshef, 2012). This assumption is particularly suitable for models where there is no selection into entry. If selection into entry is instead a desired feature of the model, then it is sufficient that the firm has a random life-time association with only one of the random variables. The other random variable may then be used to add a different element of stochasticity. In our model such element is a continuous random shock to Hicks-neutral productivity.

4 See, e.g., Manasse and Turrisi (2001), Yeaple (2005), Costinot and Vogel (2010), Helpman et al. (2010), Amiti and Davis (2011), and Burstein and Vogel (2012).

5 In our data the correlation between InRS and Inm is 0.2186.

6 Given that the probability distribution of $\phi$ and $j$ and the probability of death $\bar{\phi}$ are all constant over time, it is irrelevant for the equilibrium value of the endogenous variables whether the firm decides to stay on the basis of expected profit or on actual (instant) profit. See also the discussion in Eq. 16 in Section 9.1 of the online supplement.

7 Firms with a very high $j$ in industry $Z$ may have a higher $K$-intensity than firms with a low $j$ in industry $Y$. Yet, $A_Y > \left( \cdot \right) A_H$ is sufficient condition for the average $K$-intensity to be larger (smaller) in industry $Y$ than in $Z$. Thus, there is no average factor intensity reversal (see Section 9.2.7 of the online supplement).

8 If we had assumed that all firms survived in the market then $\hat{\psi}_c^c$ and $\beta^\ast_c$ would be the same for all $c$ and $i$; still $\hat{\beta}_i^c > \tilde{\beta}_i^c$. 

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Two firms are called twin firms if they have the same $\kappa$, the same $\phi$, and belong to different countries and industries.

**Definition 3.** A firm is K-intensive if $\kappa(\beta) > 1$. A firm is L-intensive if $\kappa(\beta) < 1$.

**Definition 4.** Let $\mu(a, \phi, \kappa)$, be an index of comparative advantage of firms defined as the marginal cost of a firm relative to the marginal cost of the average firm,

$$\mu(a, \phi, \kappa) = \frac{m_c^a}{m_c^i} = \phi^{-1}\left(1 + \phi \kappa\right)^{\frac{1}{\gamma}}. \quad (6)$$

We say that a firm has a comparative advantage over another firm iff it has lower relative marginal cost. We can now state the following theorem.

**Theorem 1.** A firm has a comparative advantage on its twin if and only if it is intensive in the factor intensively used in its industry and of which its country is relatively well endowed. In our notation:

$$\mu\left(a^b, \phi, \kappa\right) \leq \mu\left(a^j, \phi, \kappa\right) \quad \text{as } \kappa \geq 1, \text{for any } \phi. \quad (7)$$

**Proof.** See Section 2 of the online supplement. ■

Thus, for instance, a K-intensive firm ($\kappa > 1$) has a comparative advantage over its twin if it is in the K-intensive industry of the K-abundant country. Likewise, mutatis mutandis, for twins with $\kappa < 1$.

**Theorem 1** relates firm comparative advantage to country comparative advantage. Thanks to heterogeneity in factor intensity we can observe HO comparative advantage in action, as it gives rise to the comparative advantage of firms. Indeed the ranking of $\mu(-)$ (the index of comparative advantage of countries) determines the ranking of $\mu(a, \phi, \kappa)$ (the index of comparative advantage of firms). Verifying the existence of this relationship in the data provides a new empirical verification of the HO theory which goes to the very heart of the HO functioning mechanism.

Incidentally, note that the inequality (7) depends on $\kappa$ but does not depend on $\psi$. Indeed, using Eqs. (1), (3) and (6) shows that $\phi$ cancels out of Eq. (7). As it is obvious, Hicks-neutral productivity differences are irrelevant to the comparative advantage of the firms.

For our empirical purposes we shall use the following proposition. Let $RS(a, \phi, \kappa)$ denote relative sales, i.e., the sales of a firm relative to the average firm in the same industry and country. It is well known that with Dixit–Stiglitz preferences, relative sales are equal to relative marginal cost powered to 1 minus the elasticity of substitution between varieties (see Eq. (14) in Section 9.1 of the online supplement). Thus, using Eq. (6) we obtain

$$RS(a, \phi, \kappa) = \phi^{c-1}\left(1 + \phi \kappa\right)^{\frac{1}{\gamma}}. \quad (8)$$

Lastly, let $B_{\kappa} = \left\{ k : \kappa = \left(\beta_i^a/\beta_i^c\right)^{\alpha-1} \wedge \beta_i^a \leq \beta_i^c = \infty \right\}$, and let the set $B$ be the intersection of the four sets $B_{\kappa}$. Since we compare twin firms we consider values of $\kappa \in B$. Then:

**Proposition 1.** The function $RS: A \times B \rightarrow \mathbb{R}^+$ is strictly log-supermodular in $(a, \kappa)$. Further, for twin firms

$$RS\left(a^j, \phi, \kappa\right) \leq RS\left(a^j, \phi, \kappa\right) \quad \text{as } \kappa \geq 1, \text{for any } \phi. \quad (9)$$

**Proof.** See Section 9.2.3 of the online supplement. ■

**Proposition 1** says that for any pair of twin firms, the firm which is intensive in the factor intensively used in its industry and of which its country is relatively well endowed has larger relative sales. Note, again, the irrelevance of Hicks-neutral productivity difference, $\phi$, which cancels out of Eq. (9).

**Fig. 1** offers a graphical representation of the relationship between relative sales ($RS$) and relative K-intensity ($\kappa$) stated in **Proposition 1**.

Intuition for **Proposition 1** is provided by analyzing the two underlying mechanisms giving rise to it, which we do next.

1. Factor-intensity and industry technology. The first mechanism relates firm factor intensity ($\kappa$) to the technology of the industry ($A_i$). Consider two equally K-intensive firms in the same country but in different industries. Although these firms have same $\kappa$, the relative marginal cost is lower and relative sales are higher for the firm in the K-intensive industry, because the factor whose relative marginal productivity is higher for both firms with respect to the industry average ($K$) is used more intensively in the K-intensive industry. Consider now two equally L-intensive firms in the same country but in different industries. The relative marginal cost is higher and relative sales lower for the firm in the K-intensive industry, because the factor whose relative marginal productivity is lower for both firms with respect to the industry average ($K$) is intensively used in this industry.

Formally: $RS(a^j, \phi, \kappa) \leq RS(a^j, \phi, \kappa)$ as $\kappa \geq 1, \text{for any } \phi$.

2. Factor intensity and factors abundance. The second mechanism relates firm factor intensity ($\kappa$) to countries’ relative factors endowments via relative factors price ($\alpha$). Consider two equally K-intensive firms in the same industry but in different countries. Relative marginal costs are lower and relative sales are higher for the firm in the K-abundant country, because the factor that both firms use intensively with respect to the industry average ($K$) is relatively cheaper in the K-abundant country. Consider now two equally L-intensive firms in the same industry but in different countries. The relative marginal cost is higher and sales lower for the firm in the K-abundant country, because the factor that both firms save with respect to the industry average ($K$) is relatively cheaper in the K-abundant country.

Formally: $RS(a^j, \phi, \kappa) \leq RS(a^j, \phi, \kappa)$ as $\kappa \geq 1, \text{for any } \phi$.

We conclude this section with the following proposition.

**Proposition 2.** When heterogeneity is only Hicks-neutral, relative sales do not depend on country–industry characteristics.

**Proof.** Assume $\beta$ to be constant and identical for all firms, then $\kappa = 1$. Thus, from Eq. (8) we have

$$RS(a, \phi, 1) = \phi^{c-1} \quad (10)$$

which proves the proposition. ■

**4. Empirical implementation**

In the empirical analysis a firm is an element of our dataset and is identified by the index $i$. To every firm $i$ in country $c$ and industry $i$ there correspond a relative Hicks-neutral component of $TPP(a^i|\xi) = \phi(a^i|\xi)/\phi$, and a relative K-intensity $\kappa(\xi) = \theta_i^c/\theta_i^a$. From Eq. (8) the log of relative sales of firm $i$ is given by:

$$\ln RS(i) = (c-1)\ln \phi(a^i) + \frac{1-a}{1-c} \ln \left[1 + \kappa(\xi)a^i\right]. \quad (11)$$

We use the data described in Section 5 to estimate Eq. (11) over different groups of countries and industries.
In Section 6 we instead estimate a non-structural log-linear formulation of Eq. (11):
\[
\ln R S(\xi) = r_0 + r_1\ln c(\xi) + \epsilon + e(\xi),
\]
where \(r\) is an intercept and \(e(\xi)\) is an error term. The dependant variable is the sales of a firm \(\xi\) relative to its country–industry average. The first term on the right hand side is the relative Hicks-neutral productivity of \(\xi\), and the second term is its relative \(K\)-intensity. According to the model the estimated value of the coefficients \(r_0\) should be larger for \(K\)-intensive industries and \(K\)-abundant countries. This non-structural approach is particularly useful to verify the validity of each constitutive mechanisms of Proposition 1. It also provides an empirical assessment not only of our model but, potentially, of an entire class of models exhibiting heterogeneity in factor intensity.

In Section 7 we proceed to a structural non-linear estimation of Eq. (11) which gives estimated values of \(c\) and \(d_0\). According to Proposition 1 we should find that the estimates \(d_0\) are larger for \(K\)-intensive industries and \(K\)-abundant countries.

5. Data

Our empirical examination combines two main sources of data: firm-level balance sheets and country-level capital and labor endowments. Firm-level data are provided by Bureau Van Dijk’s Amadeus database. Amadeus compiles balance sheet information for a very large number of companies located in 41 European countries. Its coverage is increasing progressively. To get the most comprehensive database, we use the most recent year available at the time of writing, 2007. We proxy the capital intensity by the ratio of total assets to total employment. Sales is measured by the turnover of the firm, without distinction between exports and domestic sales. Firms in Amadeus are classified according to their primary activity. Each company is assigned to a single 3-digit NACE-Rev2 code. We restrict our empirical analysis to manufacturing sectors (including agrifood), i.e., to firms with a primary activity code between 101 and 329.\(^{11}\) We keep firms with more than one employee and non-extreme values of capital intensity (we drop firms whose \(K\)-intensity is 200 times larger or 200 times smaller than the country–industry median). Moreover, we drop all country–industry pairs which contain too few observation to perform robust regressions. We fix arbitrary limits and retain countries with more than 300 firms, industries with more than 50 active firms in 5 countries at least, and country–industry pairs with more than 5 firms.

Capital abundance for each country (\(K' LI\)) is derived from several sources. We use ILO and United Nations data for workforce figures. Capital stocks are estimated by the perpetual inventory method, using investment data from the World Bank and national sources.\(^{12}\) Industry-level capital intensity is computed directly with our data. For each country and industry, we compute the average firm-level capital–labor ratio, weighted by firms' sales. Then, \(K\)-intensity for industry \(i\), \((K/L)_i\), is the industry-level average of these values across all countries, weighted by countries' output in industry \(i\).

Finally, we need a measure of \(d_0(\xi)\). Here, we are strongly constraint by the data. The Amadeus database provides firm-level information for a quite large number of countries and industries, which is crucial for us because our identification strategy is based on a comparison, across country–industry pairs, of the magnitude of the relationship between firm-level relative \(K\)-intensity and relative sales. But, unfortunately, this database contains many missing observations, so that we can rely on a very small number of variables to estimate the Hicks-neutral component of TFP. Given these restrictions, we propose a simple methodology based on the estimation of a CES production function allowing for the existence of factor-biased productivity. Letting \(\beta_1 = 1V (i, e_0)\), Eq. (5) gives \(d_0(\xi) = [d'_0(\xi)/\bar{v}]^{1/(1-\gamma)}\).\(^{13}\) To compute \(d_0(\xi)\) from the observed capital intensity, we have to pin down \(\alpha\). We obtain this parameter from Eq. (2). Consistently with our framework, we assume that \(\alpha\) is the same for all industries, and that all firms in a given country face the same factor prices. Then, taking log and first difference (between 2006 and 2007) of Eq. (2), \(\alpha\) is obtained by regressing the first difference of the firm-level relative capital intensity on the first-difference of the relative input prices \(o_\ell = w_\ell/\ell\). We compute the national manufacturing wage, \(w_\ell\), by averaging at the country-level the individual wages reported in the Amadeus dataset. We take the price of investment goods from the Penn World Tables as a proxy for \(r\), which is also used to deflate the firms' assets.\(^{14}\) This estimation gives a \(\alpha\) of 1.2079, which is used to compute \(d_0(\xi)\).\(^{15}\) The last step consists in plugging the \(d_0(\xi)\) and the estimated \(\alpha\) to recover the Hicks-neutral productivity from a non-linear estimation of the CES production function with factor-biased productivity. This production function is estimated for each industry separately to allow the sectoral \(K\)-intensity to vary across industries.

The final database is a panel of 300,864 firms in 95 industries and 21 European countries.\(^{16}\) The country–industry panel is unbalanced because all of the 95 industries are not active in all countries. We have data for 1490 country–industry pairs, for a total of 1995 possible combinations. The average number of firms per country–industry pair is 1571, but the population within each group varies greatly. The median country–industry pair has only 796 firms, and the largest group contains 8024 observations.\(^{17}\)

6. Non-structural estimates

Table 1 reports estimates from our firm-level regressions corresponding to Eq. (12). All regressions include country–industry fixed effects. Column (1) regresses firms' relative \(K\)-intensity on firms' relative sales. The positive and very significant coefficient shows that firms with higher relative \(K\)-intensity have significantly higher relative sales. A firm with a \(K\)-intensity 10% above the country–industry mean would have relative sales that are 3.3% higher than the average firm. Column (2) introduces firms' relative \(d_0\). Not surprisingly, Hicks-neutral productivity has a great influence on firms' performances. The coefficient on the relative Hicks-neutral productivity is highly significant and very large in magnitude. The introduction of this variable also improves greatly the global fit of the regression, multiplying the \(R^2\) by a factor of 5. Column (3) verifies more directly the log-supermodularity of the RS

\(^{13}\) As already discussed above assuming \(\beta_1 = 1V (i, e_0)\) leaves the unchanged, see also Section 9.2.1 of the online supplement.

\(^{14}\) In order to control for possible endogeneity between the annual change in the aggregate wage and the firm-level capital intensity, and to alleviate measurement errors, we instrument the log change in the factor price ratio \(w_\ell/\ell\) by the initial level of this variable. In this regression, we also restrict the sample of firms to the ones that serve to compute national-level wages, i.e. the ones that are present in Amadeus in both 2006 and 2007 and report non-missing wages for these two years.

\(^{15}\) The point estimate for \(\alpha\) is larger than one, which implies substitutability between labor and capital. However, with standard errors clustered at the country level, it is not statistically different from 1, while significantly positive. Our estimate is larger than most of the estimates reported in the existing literature, which generally concludes in favor of a complementarity between the two factors (see Chirinko, 2008 for a survey). Nevertheless, our \(\alpha\) is smaller than the highest estimates surveyed in Chirinko (2008). It is also consistent with the vast literature which finds evidence that sales are positively correlated with the \(K\)-intensity of the firm; this positive correlation implies \(\alpha < 1\). Lastly, \(\alpha = 1\) is consistent with our findings reported below in Table 1 which shows a positive impact of relative \(K\)-intensity on relative sales. See Section 9.2.5 of the online supplement for the discussion on complementarity and substitutability of factors.

\(^{16}\) Belgium, Bosnia and Herzegovina, Bulgaria, Croatia, Czech republic, Estonia, Finland, France, Germany, Hungary, Italy, Latvia, Poland, Portugal, Romania, Serbia, Slovakia, Slovenia, Spain, Sweden and Ukraine.

\(^{17}\) Spain, "manufacture of structural metal products".
function interacting the firm-level relative $K$-intensity with the product of the relative $K$-abundance of the country and the relative $K$-intensity of the industry. The coefficient on the interaction term is significantly positive, which supports our main theoretical prediction summarized in Proposition 1: the marginal impact of firms' relative $K$-intensity on firms' relative sales is larger in $K$-intensive industries of $K$-abundant countries. Column (4) replicates the same exercise but interacting the relative $K$-intensity of the firm with dummies characterizing $K$-intensive industries and $K$-abundant countries instead of a continuous variable. We assign each firm to one of three mutually exclusive groups. The first group contains firms in countries whose $K$-abundance is above the median and in industries whose $K$-intensity is above the median. We shall refer to this sub-sample as the KK-group. Similarly, the LL-group contains firms belonging to countries with lower-than-median $K$-abundance and industries with lower-than-median $K$-intensity. The last group contains all remaining firms; these firms belong to either $K$-intensive industries of $L$-abundant countries or to $L$-intensive industries of $K$-abundant countries. The three coefficients associated with these interaction terms are significantly positive and, more importantly, they rank as predicted by Proposition 1: higher relative capital intensity has a stronger marginal impact in the KK-group than on the LL-group. Columns (5) and (6) replicate the tests shown in Column (2) on the KK-group and the LL-group separately. Here, by letting all the coefficients to vary across groups of country–industry pairs, we explicitly control for the possible influence of heterogeneity in $\varsigma$ across country–industry groups on the marginal effect of firms' $K$-intensity on firms' sales. The results confirm the ones shown in Columns (3) and (4). The estimated coefficient on relative $K$-intensity is significantly larger for the KK-group than for the LL-group, as expected. The coefficient on the relative Hicks neutral productivity term is also significantly larger for the KK-group. This result, which runs against Proposition 2, seems to reveal a composition effect across industries with different $\varsigma$. We now move to testing each of the two mechanisms giving rise to Proposition 1. We do this in a two-steps procedure. The first step consists in estimating the non-structural Eq. (12) separately for each country–industry pair and collecting the corresponding estimated coefficients on firms’ relative $K$-intensity. In a second step, we test whether these estimated coefficients, $\psi_i$, vary with the industry-level $K$-intensity and the country-level $K$-abundance. According to mechanism 1, we expect $\psi_i$ to be significantly larger for $K$-intensive industries. Similarly, mechanism 2 suggests a positive relationship between $\psi_i$ and countries’ $K$-abundance.

Estimates of Eq. (12) for each of the 1490 country–industry pairs are quite robust. Only 13 country–industry pairs (0.9%) show an unexpected significantly negative coefficient $\psi_i$. In 594 cases (39.9%), the coefficient is not significantly different from zero at the 10% level (130 are negative, and 473 are positive). Finally, we obtain significantly positive coefficients for a majority of country–industry pairs (883 cases, representing 59% of the country–industry pairs). The econometric tests of the two mechanisms are shown in Table 2. The top half of the table tests the validity of mechanism 1. Here, the estimated slope of the relationship between firms’ relative $K$-intensity and firms’ relative sales, $\phi_i$, is regressed on industry-level capital intensity and country fixed effects. Columns (1) and (2) show regressions performed using all $\psi_i$. Columns (3) and (4) retain only significantly positive $\psi_i$. Because our dependant variable is an estimated parameter, our standard errors are likely to be affected by heteroscedasticity. We fix this problem in Columns (2) and (4). These columns report weighted least squares estimates with weights equal to the inverse of the standard error reported for each $\psi_i$ (Saxonehouse, 1976). The positive coefficients shown in all columns of the top panel explicitly validate Mechanism 1 of Proposition 1. They confirm that, in a given country, the positive impact of relative $K$-intensity on relative sales is stronger the higher the $K$-intensity of the industries. Empirical tests of mechanism 2 of Proposition 1 are shown in the bottom half of Table 2. Here, we regress $\phi_i$ on countries’ $K$-abundance and industry fixed effects. Again, the positive coefficient on $K$-abundance in all columns supports Mechanism 2 of Proposition 1. In a given industry, the positive impact of relative $K$-intensity on relative sales is stronger the higher the $K$-abundance of the country.

7. Structural estimates

In this section, we present the results of the structural estimation of our model, based on Eq. (11). Again, the dependant variable, lnBS($\xi$), is the log of firms’ total sales relative to the corresponding country–industry average. The right-hand side variables are the Hicks-neutral productivity and the capital intensity of this firm, both relative to the country–industry averages. The parameters of this equation are $\varsigma$, $\alpha$ and $\phi_i$. Eq. (11) can be estimated with non-linear least squares. Since $\phi_i$ and $\alpha$ cannot be identified independently, we impose $\alpha = 1.2079$, which is the estimated value we have used to compute firms’ Hicks-neutral productivity.

The model requires $\phi_i > 0$ and $\varsigma > 1$. More importantly, according to Proposition 1, $\phi_i$ should be bigger for $K$-abundant countries and $K$-intensive industries than for $L$-abundant countries and $L$-intensive industries.

Estimation results are shown in Table 3. Column (1) reports the estimates for all firms in our sample. In Column (2) we impose the same $\varsigma$ for all countries–industry pairs but we interact $\kappa(\xi)$ in Eq. (11) with

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18 The coefficient for firms in the No $K$–No $L$ group should lie in between the other two coefficients. The point estimate of this coefficient does but the confidence interval overlaps with that of the LL-group.

19 The coefficients $\phi_i$ range between −0.525 and 2.599, with a mean of 0.30 and a median of 0.26.
Table 1
Impact of relative Hicks-neutral productivity and K-intensity on relative sales: non-structural log-linear model.

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Countries</td>
<td>All</td>
<td>All</td>
<td>All</td>
<td>All</td>
</tr>
<tr>
<td>Industries</td>
<td>All</td>
<td>All</td>
<td>All</td>
<td>All</td>
</tr>
</tbody>
</table>

Dependent variable: ln firms’ relative sales, ln(RSᵢ(ξ))

ln(c₁(ξ)) 1.0769⁺ (0.011) 1.0484⁺ (0.015) 1.0769⁺ (0.011) 1.1258⁺ (0.017) 0.9701⁺ (0.029)

ln(c₂(ξ)) 0.3329⁺ (0.009) 0.2064⁺ (0.008) 0.1502⁺ (0.010) 0.2682⁺ (0.011) 0.1600⁺ (0.017)

ln(c₃(ξ)) × K-intensity × K-abundance 0.0462⁺ (0.005)

ln(c₄(ξ)) × 0.2754⁺ (0.012) 0.183⁺ (0.010) 0.1537⁺ (0.017)

No KK-No LL ln(c₅(ξ)) 300,864 300,864 300,864 89,635 34,048

F-test (\(\frac{\text{ln}(\text{c}_1(\xi))}{\text{ln}(\text{c}_2(\xi))}\)) 21.98 25.79

R² 0.077 0.289 0.391 0.406 0.365

Notes: \(\xi(\xi)\) is the Hicks-neutral productivity of firm \(\xi\) relative to the country–industry average. \(\xi(\xi)\) is the K-intensity of firm \(\xi\) relative to the country–industry average. Country–industry fixed effects for all columns. Robust standard errors adjusted for country fixed effects in parentheses. Within R² are reported. Significance levels: \(^p < 0.01\). The F-tests test the equality of the estimated coefficients on the relative Hick-neutral productivity and the relative K-intensity reported in Columns (5) and (6).

Table 2
Verification of mechanisms 1 and 2 of Proposition 1.

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
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<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test of mechanism 1</td>
<td>2.118⁺ (0.386)</td>
<td>2.759⁺ (0.526)</td>
<td>3.050⁺ (0.334)</td>
<td>3.347⁺ (0.329)</td>
</tr>
<tr>
<td>Industry K-intensity</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Observations</td>
<td>1490</td>
<td>1490</td>
<td>771</td>
<td>771</td>
</tr>
<tr>
<td>R²</td>
<td>0.868</td>
<td>0.868</td>
<td>0.941</td>
<td>0.941</td>
</tr>
<tr>
<td>Fixed effects</td>
<td>Country</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Test of mechanism 2

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test of mechanism 2</td>
<td>2.751⁺ (0.359)</td>
<td>2.357⁺ (0.160)</td>
<td>2.551⁺ (0.335)</td>
<td>2.315⁺ (0.146)</td>
</tr>
<tr>
<td>Country K-abundance</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Observations</td>
<td>1490</td>
<td>1490</td>
<td>883</td>
<td>883</td>
</tr>
<tr>
<td>R²</td>
<td>0.920</td>
<td>0.940</td>
<td>0.927</td>
<td>0.954</td>
</tr>
<tr>
<td>Fixed effects</td>
<td>Industry</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: Robust standard errors in parentheses. Significance levels: \(^p < 0.01\). Overall R² are reported. Regressions in Columns (2) and (4) are performed with weight = 1, i.e., \(\omega_i\). Regressions in Columns (1) and (3) are unweighted. Columns (3) and (4) retain only significantly positive \(\psi_i\).

8. Conclusion

In this paper we have shown that the comparative advantage of countries gives rise to the comparative advantage of firms. Two otherwise identical firms (twin firms) have different relative sales if they belong to different industries or countries. This result is due to two distinct mechanisms: the interaction between relative factor intensity and industry technology and between relative factor intensity and factors endowment. These results do not require any assumption about the direction of the technology bias (if any), or about the relationship between productivity and factor intensity.

We have verified empirically the predictions of the model using firm-level data using two different samples of the same dataset. All predictions are confirmed by the empirical evidence: the comparative advantage of a firm is found to be related to the comparative advantage of the country. Each constitutive mechanism of this relationship also finds support in the data. These results contribute to the literature in two ways: they provide the first firm-level verification of the HO model and show that country comparative advantage begets a comparative advantage at firm level. Undoubtedly, Heckscher–Ohlin mechanisms not only shape international specialization but also influence firm-level performance.

Firms, countries and industries; our work has studied the theoretical and empirical interactions between these three protagonists of international trade.

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Note: \(^{20}\) Note that these coefficients are very close to the estimates reported in Columns (5) and (6) of Table 1 where, according to Eq. (12), the coefficient on \(\text{ln}(\text{c}_1(\xi))\) should be equal to \((\xi - 1)\).
Table 3
Impact of relative Hicks-neutral productivity and K-intensity on relative sales: structural estimates of Eq. (11) — sample 1.

<table>
<thead>
<tr>
<th>Countries</th>
<th>Dependent variable: ln firms’ relative sales (ln(R/S(\xi)))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Industries</td>
<td>All</td>
</tr>
<tr>
<td>(1)</td>
<td>(2)</td>
</tr>
<tr>
<td>&lt;</td>
<td>2.231\textsuperscript{a}</td>
</tr>
<tr>
<td>a\textsubscript{i}</td>
<td>0.025\textsuperscript{a}</td>
</tr>
<tr>
<td>(0.002)</td>
<td>(0.006)</td>
</tr>
<tr>
<td>a\textsubscript{i} × KK-group</td>
<td>0.064\textsuperscript{a}</td>
</tr>
<tr>
<td>(0.009)</td>
<td></td>
</tr>
<tr>
<td>a\textsubscript{i} × No KK−No LL</td>
<td>0.022\textsuperscript{a}</td>
</tr>
<tr>
<td>(0.002)</td>
<td></td>
</tr>
<tr>
<td>a\textsubscript{i} × LL-group</td>
<td>0.011\textsuperscript{a}</td>
</tr>
<tr>
<td>(0.001)</td>
<td></td>
</tr>
<tr>
<td>R\textsuperscript{2}</td>
<td>0.369</td>
</tr>
<tr>
<td>Observations</td>
<td>300,864</td>
</tr>
</tbody>
</table>

Notes: Eq. (11). Non-linear least squared. Starting values: a\textsubscript{i} = 1 and < = 2. Robust standard errors adjusted for country–industry clusters in parentheses. Significance level: *p < 0.01.

Appendix A. Supplementary data

Supplementary data to this article can be found online at http://dx.doi.org/10.1016/j.jinteco.2013.09.002.

References


Imbs, Jean and Isabelle Méjean (2012), Elasticity Optimism, mimeo.


